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Electrical and Computer Engineering
Mechanical Engineering
Systems Engineering

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ENG ME/SE 740

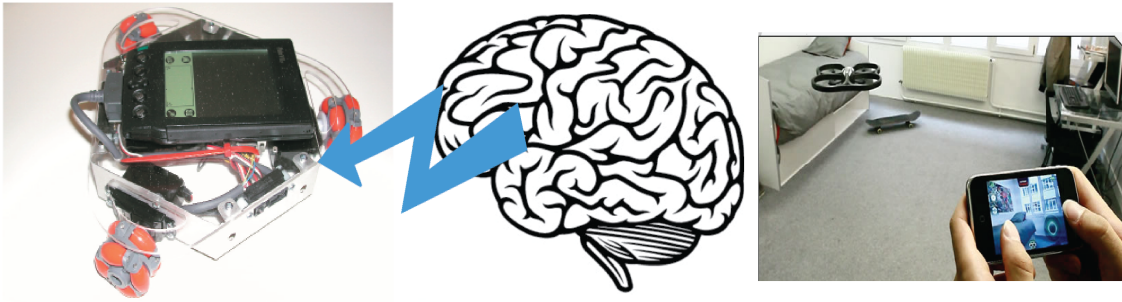
PROTOTYPE TERM PROJECTS IN INTELLIGENT MECHATRONICS

Some of these projects have been done before; some have never been done. They are offered only as ideas to guide your thinking as you come up with your own project proposal.

I. Human-Robot Interface Projects:

1. New Concepts in User Interfaces for Controlling Intelligent Machines. The Apple iPad™ was introduced in mid 2010, and at this writing, more than five hundred million have been sold. That number is dwarfed by the numbers of iOS and Android smart phones now in use, and other personal technology devices abound as well. Mobile devices provide an enormous range of new opportunities for the design of user interfaces to intelligent machines. Projects that explore various aspects of these opportunities include:

- A: *Implementing a user interface that is intuitive and easy to use is challenging.* There are apps for both iOS and Android that provide beautifully intuitive interfaces for flying any of a variety of quadricopters. A possible term project is to do an extensive literature survey of human interfaces that have been implemented on various remotely piloted vehicles. The survey should include well-known systems like the Predator and Golden Hawk as well as smaller deployed systems. How could these be improved? The project should include development or extension of a personal device user interface for an actual mobile robot or quadcopter.



- B: *User interfaces for small squadrons of mobile robots or UAV's.* While the existing apps that use smart phones or other personal devices to fly a single quadricopter work very well, equivalent software that will allow a single user to control the flight of multiple UAV's remains largely undeveloped. Part of what is needed to enable such software is a conceptual framework for managing the real-time information flow from the human operator to the machines. It would be tedious for a human operator to control every motion segment of the individual UAV's. One approach to this problem is to organize all flight regimes in terms of control hierarchies in which only one UAV that is designated *leader* is directly controlled by the human operator. The remaining UAV's will then use reactive control protocols to respond appropriately either directly to the commands that are sent from the operator to the leader or to the sensed actions of the

leader. A possible term project for ME/SE 740 is to design and provide a detailed analysis of reactive protocols enabling various realistic squadron missions. For a computer scientist’s perspective on “reactive control,” see “Technical Perspective on “Reactive Control of Autonomous Drones”, *Communications of the ACM*, V. 61:10, October 2018 p. 95, DOI:10.1145/3264411.

2. Studies in the Cognitive Psychology of Human/Robot Interaction and Decision-Making.

The goal of the research involved in this topic is the understanding of methods to capture, model, and represent, human behavior in a variety of tasks involving collaborations with autonomous robots. Models of cognitive and social psychology will inform the work. A particular objective is to develop a fundamental understanding of how humans and autonomous machines can operate together to efficiently accomplish common goals. A number of specific questions can be posed and studied: There will clearly be some tasks in which humans are likely to either perform below their potential or even to make mistakes in cognition or judgment due to workload, fatigue, preconceived notions, incomplete information, inability to process available data, inattention, and boredom. Research is needed to define laboratory situations in which it is possible to study how robots might help humans to perform better in situations where such factors lead to degraded performance in making decisions. Another interesting set of questions can be asked regarding how human behavior differs from ideal decision makers in particular problem domains and whether decision aids can be designed to help people make better decisions.

Finally, there are many open questions regarding the potential of mixed teams of humans and robotic agents. The past decade has seen substantial progress in moving from direct operator control to supervisory control of autonomous systems. A primary goal of these past efforts has been to reduce the number of humans and/or the level of skill and training required to effectively manage a certain number of autonomous systems in various mission settings. Research is needed to understand how a mixed human/robotic team can operate more capably than a purely human one.

REFERENCE: [1] W. Schwarting, A. Pierson, J. Alonso-Mora, S. Karaman, and D. Rus. “Social behavior for autonomous vehicles,” in *Proceedings of the National Academy of Sciences*, 2019.

II. Math Oriented Projects:

3. Group Theory and Intelligent Mechatronics. At the beginning of the term, we’ll see how the coordinate transformations of robotics were represented in terms of elements of $SE(3, \mathbb{R})$. $SE(3, \mathbb{R})$ is an example of a *Lie group*; this is a group on which there are defined notions of dimension and differentiation. Each of the three types of one degree-of-freedom mechanical joints (revolute, prismatic, and screw) corresponds to a type of one dimensional subgroup of $SE(3, \mathbb{R})$. Group theory has provided an enormously rich source of abstractions for robotics, computer vision, and communications theory. A possible term project would be to explore the theory of robot kinematics in terms of the structure of the various subgroups of $SE(3, \mathbb{R})$. A starting point will be our class lectures as well as the material in the recommended course texts (Murray, Li, and Sastry and Lynch and Park). Research is needed to understand the use of group-theoretic methods to describe symmetries and patterns in vehicle formations. Lie group theory has also been applied in structural mechanics in recent work on the control of deformable structures. This work has reformulated Cosserat rod theory in the language of Lie groups—most specifically $SE(3, \mathbb{R})$. The so-called geometrically exact models of rods (such as Cosserat rods) treat rods as slender (one-dimensional) structures specific sets of permissible strains—typically bending, torsion, shear, and extension. How would such strains be characterized in terms of $SE(3, \mathbb{R})$ and its lattice of subgroup types? Background reading for this topic should include S. Grazioso, G. Di Gironimo, and B. Siciliano, “A geometrically exact model for soft continuum robots: The finite element deformation space formulation,” *Soft Robotics*, 2018. [Online]. Available: <https://doi.org/10.1089/soro.2018.0047>.

The class lectures will focus on representations of $SE(3, \mathbb{R})$ and its subgroups according to standard approaches using 4×4 matrices, but a highly inventive previous term project developed an alternative approach to representations based of a specific application to protein docking. See [1].

REFERENCE: [1] P. Vakili, H. Mirzaei, S. Zarbafian, I. C. Paschalidis, D. Kozakov and S. Vajda, “Optimization on the space of rigid and flexible motions: An alternative manifold optimization approach,” 53rd *IEEE Conference on Decision and Control*, Los Angeles, CA, 2014, pp. 5825-5830. doi: 10.1109/CDC.2014.7040301. Mathematical explorations along these lines make great term projects.

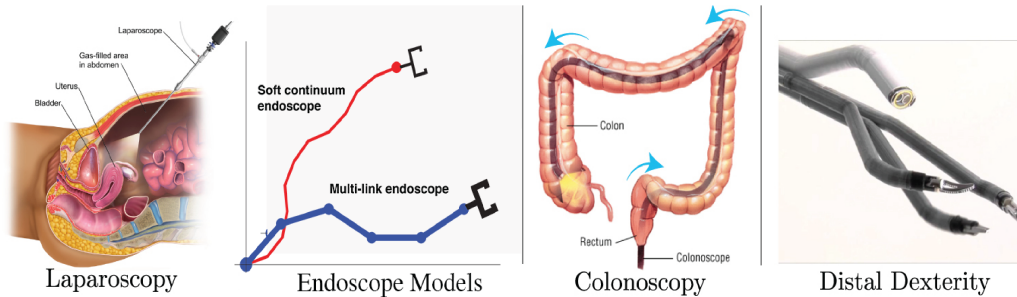
4. Nonholonomic Path Planning. Certain mechanical systems move under the influence of velocity constraints which cannot be derived from pure position constraints. (Think of the motion of an ice-skate, which can only move in a direction aligned with the blade of the skate.) Such constraints are called *nonholonomic*. Study and write a paper on motion planning for robotic devices (wheeled robots, multifingered hands grasping smooth objects, etc.) whose motions are governed by nonholonomic constraints. Special cases of current research interest involve motion planning for robots carrying dynamic loads and motion planning for groups (formations) of mobile robots. There are several largely unexplored research directions related to path planning for groups of autonomous mobile agents:

- **Accounting for dynamic constraints.** Even in the case of a single robot, planning trajectories which have timing requirements and which take account of dynamic constraints (such as limiting the amount of energy transferred to a fluid or elastic load) can be quite challenging. For groups of two or more mobile robots, trajectory planning in the face of such dynamic constraints remains an area where fundamental research is needed.
- **Accounting for intermittency in sensing and communication.** You can develop ideas, models, and simulations of multiple robot agents which are cooperatively engaged in group activities (e.g. moving through a space with obstacles) where all sensing and inter-agent communication is subject to uncertainty and intermittent disruption.
- **Efficient and reliable movement using an inventory of standard motions.** One way to deal with such intermittency is to use open-loop motions during intervals in which sensor readings and communication updates are not available. Using ideas from the *standard parts problem* (mentioned below in Paragraph 10), develop a theory of standard motions for simple nonholonomic vehicles. The goal is to have an inventory of standard motions that is sufficiently rich that a vehicle can achieve a reasonable set of motion objectives by means of concatenating standard motions. The set should also be chosen so that an efficiency criterion in terms of a reasonable control metric is met.

III. Soft Robotics:

5. Dextrous Robotic Devices Made from Soft Materials (a). Laproscopic procedures have had a transformative effect for a number of common surgical interventions—resulting in shorter hospital stays, faster recovery, and less post-operative pain for most patients. Despite notable successes in a variety of treatments, many surgeries cannot be performed laproscopically because the surgery sites cannot be reached with the existing instruments. One of the great engineering challenges is to increase the flexibility and articulation of surgical instruments so that they can be used effectively and safely in and around the soft tissues of organs in the body. A potentially impactful project would be designing a slender body mechanism with a centimeter-scale diameter and soft fluidic actuators inspired by the muscular hydrostat structure found in animal limbs like octopus arms. To obtain the necessary degrees-of-freedom, the actuators will need to be arranged in longitudinal and helical directions. The device should be passively squeezable in the radial direction, while pressurization of diagonal and longitudinal actuators will govern the roll and bending degrees of freedom in addition to modulating longitudinal stiffness. Simultaneous actuation (i.e., antagonistic contraction) can enable stiffness control, and dextrous kinematics, but the challenge is to find a design that has enough control channels (e.g., flexible tubes) to bring pressurized fluid to inflatable chambers that will actuate the movement. (See also Paragraph 12 below.)

Soft Endoscopes for Medical Interventions



6. Dexterous Robotic Devices Made from Soft Materials (b). Buckling of slender rods under various types of loading has been studied for centuries. Recently, researchers have become interested in buckling phenomena in structures that are embedded in materials other than air or water. (See, e.g., A. R. Mojdehi, B. Tavakol, W. Royston, D. A. Dillard, and D. P. Holmes, “Buckling of elastic beams embedded in granular media,” *Extreme Mechanics Letters*, vol. 9, pp. 237–244, 2016.) New theories and models of buckling are essential to understanding how to control soft endoscopes inside the lumen of an organ in a living animal. Using appropriate models of soft endoscopes, perhaps along the lines of Grazioso et al. as referenced in Paragraph 3 above, develop models of buckling in the presence of physical constraints as would be encountered with the endoscope is enclosed within the lumen of an intestine.

IV. Computer Science Meets Neuroscience Meets Control Theory

7. Cloud Based Robotics—Robot projects using AWS RoboMaker. New since last year’s version of this list of term project prototypes, Amazon Web Services (AWS) has released a cloud-based service called RoboMaker, <https://aws.amazon.com/robomaker/>. This provides a robotics development environment for application development, robotic simulation, and a robotics fleet management service that can be customized for deployment, update, and management of a user’s fleet of robots. Leveraging the capabilities of ROS (the robot Operating System) and Gazebo (simulator of mobile robots or groups of mobile robots) RoboMaker provides a simulation environment in which robot control code can be developed, tested, and actually deployed on a real robot. Robotics is one of several technologies in which Amazon is supporting developers at a variety of scales and price points. Deploying a simulated fleet of robots for applications such as search and surveillance, warehouse fulfillment, or autonomous vehicle operation would be a term project with the potential of breaking important new ground for future offerings of the course. The project will also be an opportunity to gain experience with ROS, Gazebo, and AWS Cloud9. This project will be graded on the basis of creativity and the sophistication of the simulation.

8. Develop a Foundation for the Next Generation ROS Ecosystem at Boston University. Many—if not most—people who use the B.U. Robotics Lab facilities and equipment use ROS. Together with Gazebo and Rviz, ROS has become a standard for simulations that can be ported in a straightforward way to hardware implementations. Part of the appeal of ROS is that it is open source and well documented by an active user community. (See e.g. <https://www.ros.org/>.) Aspects of ROS that are specific to Boston University are available at <http://wiki.bu.edu/robotics/index.php/Ros>. Despite the success of ROS and its broad penetration in robotics research, future advances in robot autonomy will make greater demands on real-time operation and decentralized operation of networks of multiple robots. ROS2 has been released with the aim of addressing these challenges. A term project that would be very suitable for a masters degree student aiming to pursue a *robotics specialization* would be to create some ROS2 prototype applications. The project outcomes should include one or more pages for the Robotics Lab Wiki as well as a demo that enhances one of the many available from the Web (e.g. Turtlebot 2 demo using ROS 2).

9. Theory (and Possible Experimentation) of Computer Vision for Motion Control of Autonomous Robots and UAV's. Birds and flying insects are able to perform well without using predetermined waypoints or an external position reference system. To enable true autonomy, there is a need for algorithms to localize and navigate relative to landmarks or other visually distinctive features in the environment. Algorithms of this type can be enabled by spatial representations that make use of time-to-contact and topological connectivity. Building on the work documented in

<https://hdl.handle.net/2144/15191>,

<https://hdl.handle.net/2144/27453>,

<https://www.baillieul.org/Robotics/ThesisChiaraPhilippe.pdf>,

and also the GitHub site [here](#),

a suitable ME/SE 740 project could be to develop enhance control and navigation algorithms for camera enabled robots and UAVs.

10 Neuro-Inspired Perception and Navigation. This is a project that is related to the previous paragraph. Important research remains to be done in order to understand how movement can be guided by visual perception. It is critical to realize that when moving, where we are and what is around us is not sufficient to guide navigation; we also need to know where we are coming from, i.e., account for “differences” between consecutive scenes. The goal is to develop new principles of motion control in which control signals are synthesized from very large sets of rapidly evolving input data (neurons firing in the visual cortex) and whose individual elements are too ephemeral and noisy to be useful but which turn out to be meaningful in the aggregate.

Along these lines one can pursue recent directions dealing with *principled quantization for neuromimetic control*. In an animal visual cortex, feature detectors are individual neurons—or groups of neurons—that respond to perceptually significant stimuli. Very early work on animal visual perception by Horace Barlow concluded that in the visual cortex of a frog, “on-off” ganglion cells—that respond to both the transition from light to dark and from dark to light—and also had receptive fields in the retina of a size that could detect about the size of a fly at a distance that the frog could strike. The neurobiological notions of feature saliency based on the structure of “on-off” ganglion cells in receptive fields has been reinterpreted in computer vision in a variety of well known algorithms such as SIFT, SURF, BRISK, FAST, and ORB. There have been many success stories of applications to object recognition, image registration for stereo and 3D reconstruction, and to motion detection and optical flow. At the same time, we encounter examples of visual settings in which the algorithms break down—including featureless environments (e.g., uniformly white or gray walls or scenes with uniformly textured surfaces such as the open ocean). A deeper understanding of the effects of noise and other aspects of environmental settings is needed in order to understand the challenges of visual sensing for autonomous robot navigation. A possible approach is to model the sensitivity of photo receptors in the eye to reflect the gray-scale acuity surrounding the fovea according to the exponential intensity law e^{-r^2} . For any finite dimensional linear system that observes its state by tracking every pixel in its field of view, it may be possible to design an observer with multiple channels whose multiplicity in the continuum limit becomes infinite. Ideas along these lines have recently been published for Kalman filter like models of point sensing for a heated rod, <http://arxiv.org/abs/2104.01706>. In the case of finite dimensional approximations, there is much that is yet to be understood about the theory of linear systems in which inputs and outputs are quantized and the numbers of output (observation) channels and input channels far exceeds the dimension of the state to be controlled. (See, for instance, <http://arxiv.org/abs/2104.12926>.)

11. Neuro-Inspired Motion Control. The most important application domain in which multiplexing and resource allocation over short time scales is central is in biological motion control. Brain networks and neuroscience-physiological networks are interconnected assemblages of neurons that collectively accomplish sensing, decision-making, and recruitment of muscle groups despite having strictly limited capability when acting alone. Current research is aimed at modeling and understanding *sensorimotor* feedback control in which streams

of data come from large arrays of sensors (e.g. photo-receptors in the eye) and actuation requires coordination of large numbers of actuators (e.g. motor neurons). A starting point for studying neuro-inspired motion control could be optic flow based navigation. A number of widely used algorithms in the OpenCV library can be used (in concert) to extract steering signals from the motions of image pixels on the focal plane of a video camera. The challenge in synthesizing a robust and reliable steering signal is frame-to-frame matching of features in the presence of noise, drop-outs, and lack of persistence for more than a small number of frames. For higher animals, from mice to primates, the key to safe movement seems to be the coordination of neuronal activations in a number of different brain and neurological sites—including the visual cortex, the prefrontal cortex (which handles decision making about where and how to move), and sites like the hippocampus and entorhinal cortex that enable spatial memory. The network architecture of neuronal interconnections both within and between these sites involves very large numbers of connections among very large numbers of nodes. Neuroscientists believe that this architecture makes the interconnected cortical networks very robust to noise, to conflicting inputs, as well as to frequent intermittent failures of individual neurons. The mechanisms by which animal behaviors are shaped by sensory input modulated by memory and conscious choice involve a poorly understood process for achieving consensus among groups of neurons in key brain regions. A number of possible robotics term projects are suggested by current research in brain science:

(1) Read the *C. elegans* paper: Nature <https://doi.org/10.1038/s41586-019-1352-7> (July 4, 2019), and invent a comparably simple (or perhaps simpler) neurological architecture that is able to produce movement and to respond appropriately to selected sensory inputs.

(2) Read E. Izhikevich *Dynamical Systems in Neuroscience*, MIT Press, ISBN 978-0-262-09043-8. Use spiking neuron models of the type that he describes to simulate activity that is found within a particular brain region (hippocampus, entorhinal cortex, . . .) or that enables communication between regions.

See also Choi *et al.* https://www.mitpressjournals.org/doi/full/10.1162/neco_a.01072.

(3) Develop a simple mathematical model of uncertainty reduction attributable to the compilation of inputs from large numbers of noisy sensors which are individually imprecise but collectively able to provide accurate estimates.

12. Research to understand the INFOMAX principle for robotic networks. Research is needed to understand general principles of how the placement of nodes in a network and the interconnections between the nodes should be arranged so as to maximize various network-specific measures of information that is collectively acquired and held by the nodes. A prototypical class of problems involves models of perception, communication and information flow between pairs of networks. A key feature in such models will be abstracted descriptions of information sources that capture common features of data from (i) spatially-distributed sensor networks, (ii) neural impulses passing among regions of the brain, and (iii) salient features of continuum data in spatially varying random fields. The fundamental problem of information flow between a source and a receptor network (e.g., a data-collecting sensor/robotic network in the case of (i) and (iii) above, and selected cortical brain regions in the case of (ii)) is to understand how the receptor network receives the maximum information available in the source network subject to operating constraints such as noise, signal-to-interference ratios, energy requirements (See Berger, 2003.) and other data-rate limiting factors. The objective of the research may be phrased as the problem of finding mechanisms that implement the *infomax* principle as proposed in the classic paper by Linsker (1988).

REFERENCES:

1. R. Linsker, “Self-organization in a perceptual network.” *IEEE Computer*, 21(3):105-317, 1988.
2. T. Berger. “Living Information Theory: The 2002 Shannon Lecture.” *The IEEE Information Theory Newsletter*, 53:1-19, 2003.

13. Data, Software, and Mathematical Foundations of Machine Learning and AI. One hundred percent of our incoming class of PhD students in Systems Engineering this year reported that their main research interest was machine learning. Some historians trace the origins of machine learning to the eighteenth century when the Reverend Thomas Bayes wrote an essay entitled “An Essay towards solving a Problem in the Doctrine of Chances.” Most people—with due respect for Bayes—would probably date the real beginnings of

machine learning to the early 1940s and 50s when work of Alan Turing and Marvin Minsky was first published—accompanied by the invention of digital computers (ENIAC, Manchester Mark I, etc.). Since its introduction, machine learning has been viewed as a potentially important enabler of robotics, but it is fair to say that it has not yet realized this potential. Several things could now change this.

As the processing capability of computers has increased exponentially for decades (in accordance with Moore’s law), radically new concepts in distributed (cloud) computing have created the Internet—a distributed digital knowledge base that could not have been imagined in 1993, the launch year of the World Wide Web. There has been an explosive proliferation of digitally archived data — both proprietary and public. A few of the ever increasing numbers of examples of publicly accessible data sets are:

(a) The CIFAR-10 dataset consisting of 60,000 32×32 color images of 10 classes of objects, with 6000 images per class, [4],

(b) 150 Mbytes of flight trajectories of *Myotis velifer* bats reconstructed from 15 Tbytes of video recordings of emergences from the Bamberger cave in Texas. (Data in [2], analysis in [1].), and

(c) The 2010-2013 New York City Taxi Data, curated by Dan Work, [3], comes with the caveat that “All . . . obvious trip errors should be discarded in any analysis. In our preliminary investigations, these errors account for roughly 7.5% of all trips.”

A few hours of web searching will yield many other interesting data sets. Large publicly accessible data sets are proliferating both because data is increasingly easy to archive and also because funding agencies are now requiring data to be included as one of the reported products of sponsored projects. (See, for instance, <https://www.nsf.gov/pubs/policydocs/pappguide/nsf15001/gpg.2.jsp#IIC2j> .)

Given this background, it is not surprising that current research in systems engineering and computer science is focused on AI in general and machine learning in particular. Some specific examples:

(i) Within the broad disciplinary domain of systems and control, the field of systems identification provides techniques for deriving mathematical models of dynamical systems based on input-output data. The most mature aspects of systems identification deal with time-invariant linear systems in which there is a convolution operator relating the input and the system’s output. The problem of sysID is to find the impulse response from observed data. Such deconvolution problems appear in many fields including biology, computer science (computer vision) physics, and engineering. While many aspects have been refined to provide a corpus of software in the Systems Identification Toolbox in MatlabTM [8], recent research has sought to make improvements through connections with machine learning techniques that have been developed independently and are focused on reproducing kernel Hilbert spaces. This research has been illuminated, among a number of ways, by applications to robot motion control, [5].

(ii) With the appearance of new cloud resources and many publicly available data sets, there has been renewed interest in neural networks as a means to recognize features in images,[4], to do so-called deep learning, [6], and to provide the basis of machine learning of languages, [7].

Term projects in machine learning and AI: What kernel methods, classical linear systems ID, and neural networks have in common is the “training” of models from data. Taking the very broad view that training simply means assimilating information, an interesting class of problems related to the methods described as well as to many more is how should we value information in terms of its usefulness in training. Some specific research questions are:

1. Are there information-based techniques that will enable methods of improving training sets - both by adding information rich examples as well as by culling and discarding elements of the training set that have little or no training value? Can networks be more efficiently trained with smaller but “better” training sets? Are there useful information-theoretic measures of the training value of data—images in particular, say?

2. Regarding the soft-robot applications described in Paragraphs 8, 9, a major challenge is to instill in the robot the ability to feel its environment. An ambitious project for the course will be to design a means of sensing deformations that can be coupled to learning techniques to have the robot recognize textures and shapes of objects within certain prescribed classes—e.g., bricks, balloons, and simulated or real animal tissue.

REFERENCES:

- [1] Zhaodan Kong, Nathan Fuller, Shuai Wang, Kayhan Özcimder, Erin Gillam, Diane Theriault, Margrit Betke, and John Baillieul, ‘ “Perceptual Modalities Guiding Bat Flight in a Native Habitat,” *Scientific Reports - Nature*, **6**, Article number: 27252 (2016). <http://www.nature.com/articles/srep27252>.
- [2] Flight data for cave emergence of *Myotis velifer*, July, 2013. John Baillieul, Curator. <http://www.baillieul.org/data/CSV/>
- [3] 2010-2013 New York City Taxi Data, Dan Work, Curator. <https://publish.illinois.edu/dbwork/open-data/>
- [4] <https://www.cs.toronto.edu/~kriz/cifar.html>
- [5] Gianluigi Pillonetto, Francesco Dinuzzob, Tianshi Chenc, Giuseppe De Nicolao, and Lennart Ljung, “Kernel methods in system identification, machine learning and function estimation: A survey,” *Automatica*, Volume 50, Issue 3, March 2014, Pages 657 - 682.
- [6] <http://caffe.berkeleyvision.org/>
- [7] Gideon Lewis-Krause, “The Great AI Awakening,” *New York Times Magazine*, Dec. 14, 2016.
- [8] <https://www.mathworks.com/help/ident/>

V. *Mechano-informatics* - The Interplay of Physics, Information Theory, and AI

14. Toward a Theory of Action-Mediated Communication. The principles of information theory (See, e.g., Cover and Thomas, *Elements of Information Theory 2nd Edition*, Wiley-Interscience; 2 edition (July 18, 2006), ISBN-10: 0471241954, ISBN-13: 978-0471241959, 776 pages.) dictate that when messages are encoded for transmission through a communication channel, symbols in a code book should be assigned to a message source in such a way that frequently occurring codewords are the shortest (require the fewest bit to express) while infrequently occurring codewords are allowed to be longer. We would like to establish a similar guiding principle for “action-mediated” communication. When the motion of a physical system is used to encode a message, there is typically an associated cost that is of interest—e.g., the energy required to produce the motion, the spatial extent of the motion, or the time that is needed to execute the motion. Thus, in using the motions of a controlled dynamical system for the purpose of communication, we will want to encode messages in such a way that the least costly motions are the ones used with the greatest frequency.

Framed in this way, the problem of optimal action-mediated communication shares common features with the *standard parts problem*, where the goal is to assemble a number (say n) of objects using an inventory of m different kinds of parts in such way that over time the averaged cost of assembling the objects is minimized. A possible term project is to explore this circle of ideas for action mediated control in the context of applications to team sport play (How do team members efficiently communicate with each other by means of the way they move on the playing field?), to dance (How do dance partners communicate with each other to chose sequences of moves that will be judged to be appealing while at the same time making maximally modest demands on the energy reserves of the dancers?), and to problems in synthetic biology where there is now interest in establishing registries of standard biological components for the synthesis of novel biological systems. References that also mention possible applications to quantum information processing include:

W. S. Wong and J. Baillieul, “Control Communication Complexity of Nonlinear Systems,” *Communications in Information and Systems*, 9:1, pp. 103-140, 2009. <http://people.bu.edu/johnb/CIS-9-1-A5-wong.pdf>

J. Baillieul and W.-S. Wong, “The Standard Parts Problem and the Complexity of Control Communication,” in *Proceedings of the 48-th IEEE Conf. on Decision and Control*, Shanghai, China, December 16-18, 2009, pp. 2723 - 2728. Digital Object Identifier: 10.1109/CDC.2009.5400

15. Communication Constrained Control. As machines and devices of all kinds have become increasingly autonomous, there has been a corresponding interest in having the devices interoperate so as to work

together on shared tasks. Networked operation of cooperating devices is key to modern transportation technologies from flight control systems on aircraft to the interconnected control processors that coordinate steering, braking, and power train functions. In many cases, actuators, sensors, and microprocessors are connected by wires (as is the case with *CAN bus* technology in automotive applications), but there is increasing interest in having them communicate wirelessly. The rates at which networked devices can communicate with each other is thus limited, and such data rate constraints in turn constrain the performance of the system. With networks of sensors, actuators and processors in mind in say late model automobiles, a possible term project could examine current wireless networking technologies like *BluetoothTM* and *ZigBee* and estimate performance limitations that can arise due to noise, packet loss, and the degree of asynchronism in the operation of nodal components of the network.

Due dates for term project elements.

1. Project proposals (one page) due no later than 2/10/22. Earlier is better.
2. Interim progress presentation due around 3/15/22. This will involve a formal class presentation in which you present
 - Why you chose this project and why it is important and interesting. (These questions should, of course, be addressed in your project proposal as well.)
 - What is the relevant background? If it is original research, what is the state of the art, and what do you hope to accomplish? If it is some type of hardware or software design, what are the main challenges going to be?
 - How has the definition or scope of your project changed in the four weeks since you submitted your project proposal?
3. Final project class presentations will be in late April. Written project reports will be due on May 3, 2022.